

Stoichiometry of LaAlO₃ films grown on SrTiO₃ by pulsed laser deposition

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We have studied the stoichiometry of epitaxial LaAlO₃ thin films on SrTiO₃ substrate grown by pulsed laser deposition as a function of laser energy density and oxygen pressure during the film growth. Both x-ray diffraction (θ - 2θ scan and reciprocal space mapping) and transmission electron microscopy (geometric phase analysis) revealed a change of lattice constant in the film with the distance from the substrate. Combined with composition analysis using x-ray fluorescence we found that the nominal unit-cell volume expanded when the LaAlO₃ film was La-rich, but remained near the bulk value when the film was La-poor or stoichiometric. La excess was found in all the films deposited in oxygen pressures lower than 10^{-2} Torr. We conclude that the discussion of LaAlO₃/SrTiO₃ interfacial properties should include the effects of cation off-stoichiometry in the LaAlO₃ films when the deposition is conducted under low oxygen pressures. © 2013 AIP Publishing LLC. [<http://dx.doi.org/10.1063/1.4811821>]

I. INTRODUCTION

Since the discovery of a high-mobility conducting layer between the TiO₂-terminated SrTiO₃ substrate and LaAlO₃ thin film by Ohtomo and Hwang,¹ the origin of this 2-dimensional electron gas (2DEG) system has been intensively studied.² Several mechanisms have been proposed including electronic reconstruction,¹⁻⁶ oxygen vacancy effects,⁶⁻¹⁰ defects due to laser bombardment,¹¹ and interfacial ion intermixing between LaAlO₃ and SrTiO₃.^{3,12,13} Recently, it has been shown both theoretically¹⁴ and experimentally^{15,16} that the transport property of the interface changes drastically when the LaAlO₃ film stoichiometry is varied. Since most of the LaAlO₃ films for the 2DEG studies were grown by pulsed laser deposition (PLD) and a wide range of growth conditions in terms of laser energy density and oxygen pressure have been used, a systematic study of the LaAlO₃ film stoichiometry as a function of PLD growth conditions is critically needed. Only few reports exist in the literature on this issue and the scopes of these studies are limited.^{17,18} In addition, although a low oxygen pressure during the film deposition can lead to oxygen vacancies in the SrTiO₃ substrate, which affect the measured transport property,⁶⁻¹⁰ it could also affect the LaAlO₃ film stoichiometry. It is important to separate the oxygen vacancy effect from that of cation off-stoichiometry in the LaAlO₃ film.

Here, we present a systematic study on the laser energy density and oxygen pressure effects on the LaAlO₃ film stoichiometry by structural and compositional analyses. In the range of the deposition parameters we have studied, we found that the LaAlO₃ film stoichiometry depends strongly on the oxygen pressure during the deposition, and not significantly on the laser energy density. The optimal oxygen pressure for stoichiometric LaAlO₃ films is about 100 mTorr.

Although the details of the result could be different for different experimental setups, our results indicate that LaAlO₃ film stoichiometry should be considered in the discussions of 2DEG properties at the LaAlO₃/SrTiO₃ interface under various deposition conditions.

II. EXPERIMENT

The LaAlO₃ thin films used in this work were grown on (001) SrTiO₃ substrates by PLD using a KrF excimer laser ($\lambda = 248$ nm, and pulse duration 25 ns) from a single crystal LaAlO₃ target. The depositions were carried out at various laser energy densities, from 0.7 to 2 J/cm², and oxygen pressures, between 0.3 and 10^{-4} Torr (the background vacuum is 10^{-5} to 10^{-6} Torr). The growth rate of the LaAlO₃ film was calibrated at the identical growth conditions prior to each growth using Dektak profilometer. The growth time was fixed at 15 min for all the films. In order to keep the total film thickness at about 100 nm repetition rate of the laser pulses was varied for each sample to accommodate the change in the growth rate, from 1.2 Hz (for laser energy density of 2 J/cm² and oxygen pressure of 300 mTorr) to 13.5 Hz (for laser energy density of 0.7 J/cm² and oxygen pressure of 10^{-2} Torr). The depositions were carried out at 730 °C substrate temperature and the samples were cooled down to room temperature after growth at an oxygen pressure of 200 Torr.

The structural properties of the deposited LaAlO₃ films were analyzed by x-ray diffraction (XRD) using a Bruker D8 Discover diffractometer. The film texture and epitaxial quality were characterized by θ - 2θ scan, azimuthal ϕ scan, and reciprocal space mapping (RSM), from which the out-of-plane and in-plane lattice constants of the LaAlO₃ films were calculated. The uncalibrated La/Al ratios presented in this paper, were determined by x-ray fluorescence (XRF) with an iXRFTM model 550 system interfaced to an FEI DB235 dual-beam scanning electron and ion beam microscope. The XRF system uses an Ag-target, an fX X-ray tube, and a

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liquid nitrogen-cooled SiLi detector. The x-ray source produces a collimated 500- μm beam spot on the sample. Quantitative analysis was performed using the EDS2008 software. Using high-resolution transmission electron microscopy (HRTEM) images, geometric phase analysis (GPA)^{19,20} was carried out to quantify the strain as a function of distance from the interface. Cross section samples were prepared via an *in situ* lift-out process using an FEI Strata DB235 focused ion beam (FIB) system,²¹ and then analyzed using a JEOL JEM2100 TEM operated at 200 kV.

III. RESULTS AND DISCUSSIONS

The PLD-deposited LaAlO₃ thin films grow epitaxially on the (001) SrTiO₃ substrates. Figure 1 shows (a) a θ - 2θ scan and (b) an azimuthal φ scan of the (103) diffraction peak for a LaAlO₃ film deposited with a laser energy density of 1.5 J/cm² in an oxygen pressure of 100 mTorr. Besides the substrate peaks, only (00L) diffractions from the film are present in the θ - 2θ scan, indicating that the *c*-axis of the film is oriented normal to the substrate surface. A Nelson-Riley fitting of the diffraction peaks gives a *c*-axis lattice constant of $3.78 \pm 0.01 \text{ \AA}$ for the film. The lattice constant can also be calculated using the SrTiO₃ peak as a reference ($a = 3.905 \text{ \AA}$). The *c*-axis lattice constant thus calculated is $3.78 \pm 0.01 \text{ \AA}$, consistent with the Nelson-Riley fitting. Figure 1(b) shows φ scans for both the LaAlO₃ film and the SrTiO₃ substrate. Both

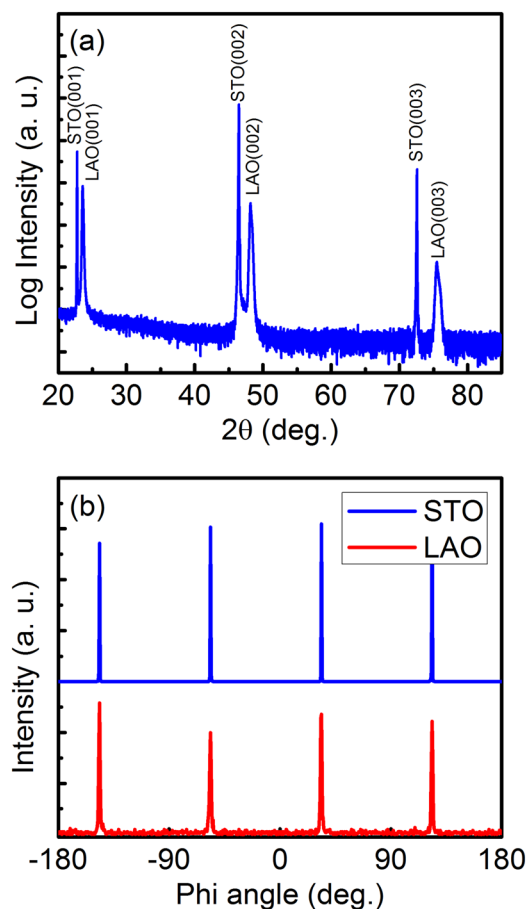


FIG. 1. Typical XRD spectra for a LaAlO₃ film. (a) A θ - 2θ scan. (b) Azimuthal φ scans of the (103) peaks of the LaAlO₃ film and the SrTiO₃ substrate.

scans show a four-fold symmetry and the film and substrate peaks overlap, suggesting a cube-on-cube epitaxial relationship LAO (100) [001]//STO (100) [001]. From the φ scan the *a*-axis lattice constant of the film is calculated to be $3.82 \pm 0.02 \text{ \AA}$, a tensile strain of 0.7% from the bulk value of 3.789 \AA . The result indicates that the epitaxial strain in the 100 nm-thick LaAlO₃ film is mostly relaxed. The volume of the pseudo-cubic unit cell of the film is 54.988 \AA^3 , a 1% expansion compared to the bulk value of 54.397 \AA^3 . The epitaxial growth shown by Fig. 1 is typical of all the films in this work except that the lattice constants are different for films deposited under different conditions.

The uncalibrated cation stoichiometry of the LaAlO₃ film in Fig. 1 was measured by XRF. Because the x-ray source for XRF is brighter than the electron beam often used in energy dispersive spectroscopy (EDS), XRF provides higher sensitivity for the elemental analysis of surfaces and thin films. In the XRF spectrum in Fig. 2, emission peaks of the characteristic secondary x-rays from La and Al in the film and Sr and Ti from the substrate are seen. The peaks were fitted with Gaussian distributions, which effectively resolved the overlap of, for example, the Ti *K α* and La *L α* peaks. The relative areas under the Gaussian peaks of La and Al, with the ZAF correction, were used to obtain the La/Al cation ratio, *x*. The *K α* peak of Al and the *L α* peak of La were chosen for all the XRF analysis in this work, although the use of the *L β* and *L γ* peaks of La provided similar results. For the film shown in the figure, the uncalibrated La/Al cation ratio from the XRF analysis is 0.91 ± 0.03 .

LaAlO₃ films deposited under different conditions were characterized by both the XRD and the XRF measurements. The laser energy densities used were 0.7, 1.0, 1.5, and 2.0 J/cm², and the oxygen pressures used were 1×10^{-4} , 1×10^{-3} , 1×10^{-2} , 1×10^{-1} , and 3×10^{-4} Torr. Since both laser energy density and oxygen pressure can affect the result, all combinations of the two parameters were studied. Figure 3 shows the XRD results for three representative films deposited with different laser energy densities and oxygen pressures, resulting in different La/Al cation ratios: (a) and (d) 0.7 J/cm², 300 mTorr, and $x = 0.62$; (b) and (e) 1 J/cm², 100 mTorr, and $x = 1.01$; and (c) and (f) 1 J/cm², 10^{-4} Torr, and $x = 1.19$. Figures 3(a)–3(c) are θ - 2θ profiles around the (002) SrTiO₃ Bragg reflection (the dashed lines represent the bulk *c*-axis lattice constant of

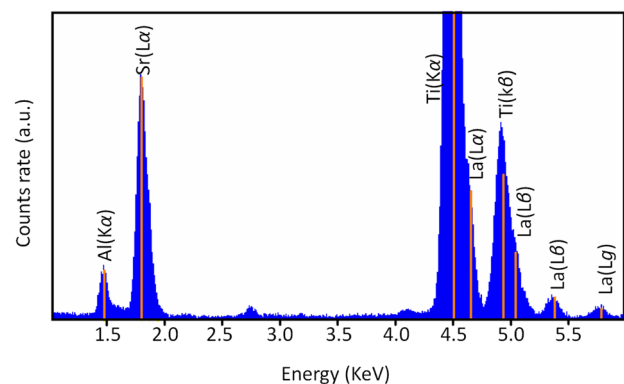


FIG. 2. XRF spectrum for the LaAlO₃ film shown in Fig. 1.

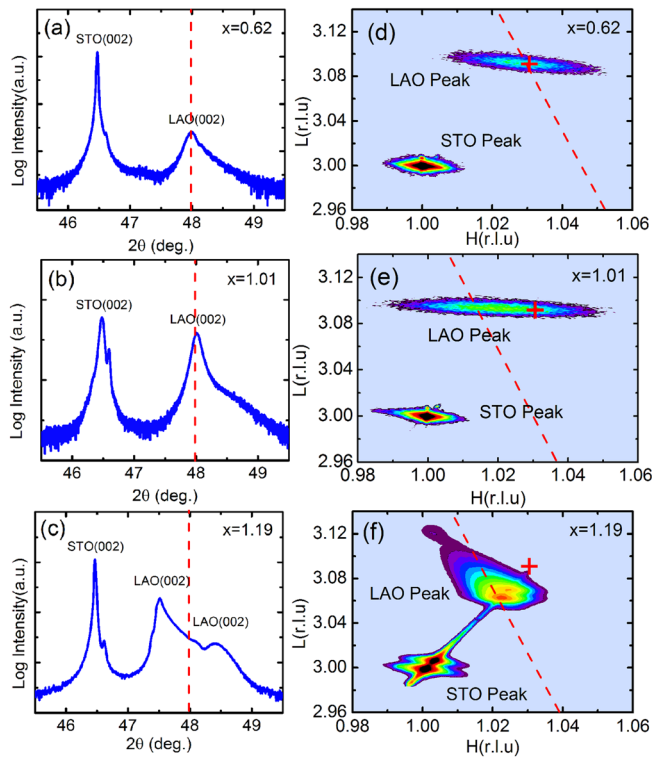


FIG. 3. XRD spectra for LaAlO_3 films with different $x = \text{La}/\text{Al}$ cation ratios deposited with different laser energy densities and oxygen pressures: (a) and (d) $0.7 \text{ J}/\text{cm}^2$ and 300 mTorr ; (b) and (e) $1 \text{ J}/\text{cm}^2$ and 100 mTorr ; and (c) and (f) $1 \text{ J}/\text{cm}^2$ and 10^{-4} Torr . Figures (a)–(c) are θ - 2θ profiles around the (002) SrTiO_3 peak and (d)–(f) are logarithmic RSM contour plots around the (103) SrTiO_3 spot. The dashed lines in (a)–(c) and the red “+” signs in (d)–(f) correspond to the values of bulk LaAlO_3 . The dashed lines in (d)–(f) are points in the reciprocal space with equal unit-cell volumes.

LaAlO_3). Figures 3(d)–3(f) are reciprocal space maps around the (103) peak of the SrTiO_3 substrate (the red “+” symbols correspond to the reciprocal point of bulk LaAlO_3). The θ - 2θ scans show broader film peaks than the substrate peak, in particular for the La-rich film, which displays a clear double-peak structure. This is confirmed by the RSM maps showing broadening of the film spots in the L direction, suggesting that the out-of-plane c -axis lattice constants of the films are not uniform across the film thickness. The peak values suggest c -axis lattice constants similar to that of the bulk LaAlO_3 for the La-poor and stoichiometric films and larger than the bulk value for the La-rich film. The non-uniformity is more severe in the a -axis lattice constant. From the RSM maps one can see significant broadening of the film spots in the H direction, with the overall in-plane a -axis lattice constants larger than that of the bulk LaAlO_3 in the near stoichiometric and La-rich films.

The broadenings of the diffraction peaks in the θ - 2θ scans and RSM contour maps are the result of strain relaxation in the epitaxially grown LaAlO_3 film, which experiences a tensile stress of 3% on the SrTiO_3 substrate. Above a critical thickness, which depends on the deposition conditions and is around 4 nm, the strain in the LaAlO_3 film starts to relax. This is revealed by the result of geometric phase analysis (shown in Fig. 4), which was performed on the LaAlO_3 film in Fig. 1.

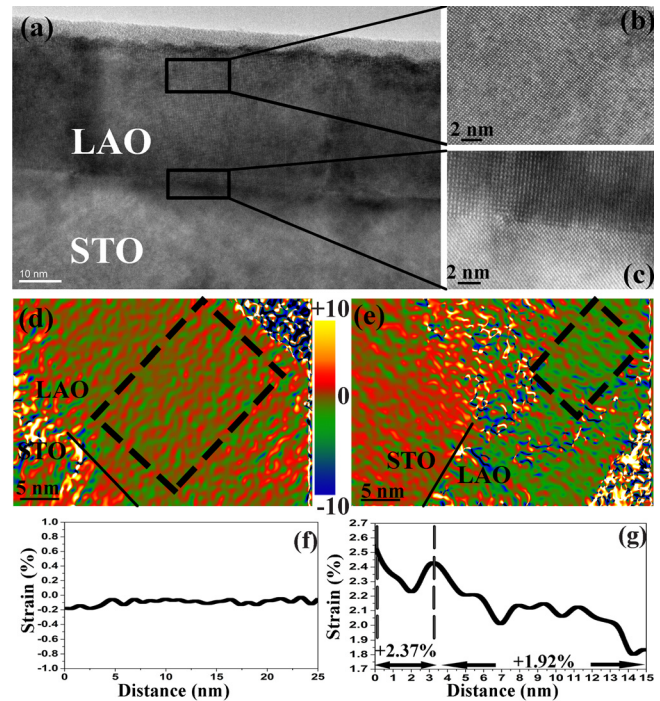


FIG. 4. HRTEM images and in-plane map of strain in parallel to the interface direction for the film in Fig. 1. (a) A low-magnification TEM image. (b) and (c) HRTEM images of the top part of the LaAlO_3 layer and its interface with SrTiO_3 , respectively. (d) and (e) GPA strain analysis of the edge of the LaAlO_3 layer and the $\text{LaAlO}_3/\text{SrTiO}_3$ interface, respectively. The dotted boxes indicate the regions which were used to measure the average strain. (f) Average strain gradients inside the dotted boxes shown in (d), where the x -axis ends at the edge of the LaAlO_3 layer. (g) Average strain gradients inside the dotted boxes shown in (e), where the x -axis starts at the $\text{LaAlO}_3/\text{SrTiO}_3$ interface.

Figure 4 illustrates the changing of strain in the LaAlO_3 film relative to its interface with the SrTiO_3 substrate. Figure 4(a) is a low-magnification TEM image of the LaAlO_3 film on top of the SrTiO_3 substrate, showing a film thickness of $\sim 100 \text{ nm}$. From Figs. 4(b) and 4(c), which illustrate HRTEM images of the top part of the LaAlO_3 layer and its interface with SrTiO_3 , respectively, one can see more contrast, indicating more strain, near the $\text{LaAlO}_3/\text{SrTiO}_3$ interface. The region indicated with the dotted box in Fig. 4(d) and the average strain profile shown in Fig. 4(f) represent insignificant strain gradient on top of the LaAlO_3 layer, which confirms its relaxation away from the interface. The average strain values on top of the LaAlO_3 layer was measured $\sim -0.06\%$, which is below the 0.1% resolution of the GPA technique. The dotted box covers the top 25 nm [x -axis in Fig. 4(f)] of the LaAlO_3 layer; therefore, the x -axis ends at the edge of the LaAlO_3 layer. Figures 4(e) and 4(g) illustrate the profile of the strain starting at the $\text{LaAlO}_3/\text{SrTiO}_3$ interface into the LaAlO_3 layer [x -axis in Fig. 4(g)]. The strain profile indicates that at the first $\sim 4 \text{ nm}$ distance from the interface, the LaAlO_3 layer is under an average tensile strain of 2.37% compared to the bulk LaAlO_3 , which decreases to 1.7% after $\sim 15 \text{ nm}$ from the interface. These results confirm the existence of strain gradient in the LaAlO_3 layer as a function of the distance from the interface toward the film surface.

The result in Fig. 3 indicates that the strain relaxation depends on the compositions of the LaAlO_3 films. The

relaxation is the most gradual in the near stoichiometric film—the in-plane lattice constant ranges from that of the SrTiO₃ substrate to that of the bulk LaAlO₃. For the La-poor film, the relaxation occurs the fastest—the coherently strained layer is too thin to be detectable by RSM and the *a*-axis lattice constant of the film is close to the bulk value. In the La-rich film, both the in-plane and the out-of-plane lattice constants vary substantially across the film thickness, with both *a*- and *c*-axis lattice constants larger than those of the bulk LaAlO₃.

Ohnishi *et al.* have shown that lattice expansion often observed in homoepitaxial SrTiO₃ films is not due to oxygen vacancies but originates from cation off-stoichiometry.²² Thus, the lattice expansion in homoepitaxial SrTiO₃ films has been used as a sensitive indicator of cation off-stoichiometry.^{22–25} Since there is no epitaxial strain in the homoepitaxial SrTiO₃ film on SrTiO₃ substrate, the increased *c*-axis lattice constant alone can represent the lattice expansion. The strain and strain relaxation in the LaAlO₃ films on SrTiO₃ make the task of correlating lattice expansion to film stoichiometry much more complex as the lattice constants vary continuously across the film thickness. Assuming that the film composition does not change throughout a film, we draw lines of equal unit-cell volume on the RSM maps and take the peak intensity values [the dashed lines shown in Figs. 3(d)–3(f)] as the nominal unit-cell volumes of the films. The two equal-volume lines passing through the half maximum intensity define the error bar. In Fig. 5, the unit-cell volume versus the La/Al cation ratio is plotted for 20 LaAlO₃ films fabricated under different conditions. The LaAlO₃ bulk value is shown as a dashed line. Despite the large error bars in the volume, a trend is evident: The unit-cell volume increases from the bulk value when the film is increasingly La-rich, reaching about 4%; for La-poor and stoichiometric films, the volume expansion is not as severe and the unit-cell volume is similar to that of the bulk LaAlO₃. While we cannot rule out the effect of oxygen vacancies on the volume expansion in the LaAlO₃ films, the result clearly shows the correlation between the cation stoichiometry and the lattice expansion. Even with

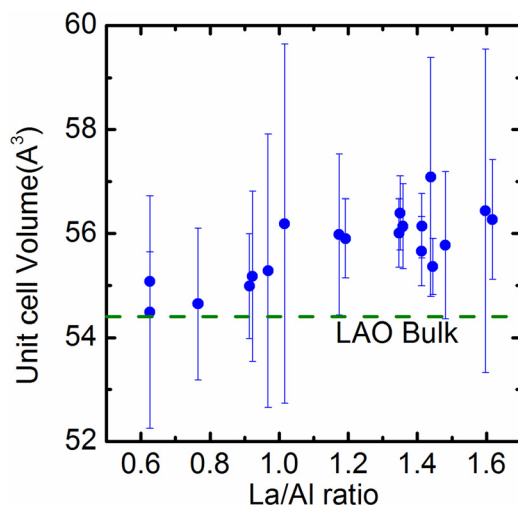


FIG. 5. Unit-cell volume of the LaAlO₃ films as a function of the La/Al cation ratio.

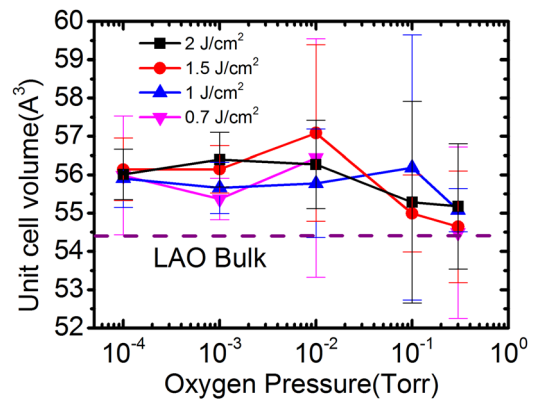


FIG. 6. Unit-cell volume of the LaAlO₃ films as a function of oxygen pressure during deposition for different laser energy densities.

the complications due to strain and strain relaxation in the LaAlO₃ film, one can use the unit-cell volume as an indication of the film stoichiometry similar to the case of homoepitaxial SrTiO₃ films. In particular, when there is excess of La in the LaAlO₃ film the lattice expands. It is, however, not effective for detecting La deficiency in the film.

Having established the correlation between the La/Al ratio and the nominal unit-cell volume of the LaAlO₃ films, we plot in Fig. 6 the unit-cell volume as a function of the oxygen pressure during the deposition for different laser energy densities. Even with the large error bars, one can see that the unit-cell volume is larger than the bulk value when the oxygen pressure is 10⁻² Torr and lower for all the laser energy densities used for the deposition. When the oxygen pressure is 10⁻¹ Torr or higher, the unit-cell volume becomes closer to that of the bulk LaAlO₃. In Fig. 7, the cation ratio of the film as measured by XRF is plotted as a function of oxygen pressure for different laser energy densities. For the films grown under the same oxygen pressure, no significant difference was observed in composition for different laser energy densities. For the lower oxygen pressures, 10⁻² Torr and lower, the cation ratio exhibits a large deviation from the stoichiometry, an excess of La by as much as over 50%. As the oxygen pressure is increased to 0.1 Torr, the deviation in the La/Al ratio becomes smaller and near stoichiometric. Further increase in the oxygen pressure resulted in La

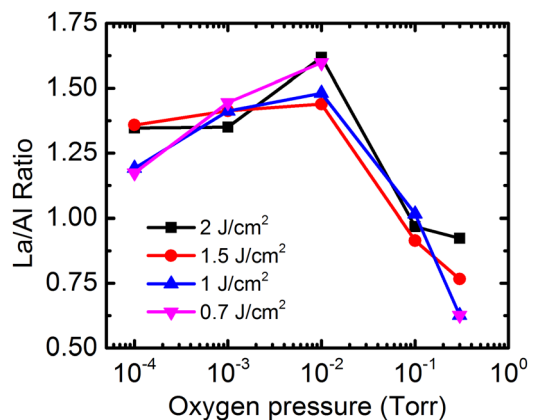


FIG. 7. The La/Al cation ratio as a function of oxygen pressure for different laser energy densities.

deficiency, which cannot be detected effectively by the unit-cell volume.

The result presented here shows that the composition of the PLD deposited LaAlO₃ films depends on the deposition conditions. When the oxygen pressure during the deposition is lower than 10⁻² Torr, the film becomes La-rich. The optimal oxygen pressure for film stoichiometry is about 10⁻¹ Torr. Our result may have significant implications for the study of the 2DEG at the LaAlO₃/SrTiO₃ interfaces. As most of the reported studies of the LaAlO₃/SrTiO₃ interfacial properties used LaAlO₃ films deposited at 10⁻² Torr oxygen pressure or lower, these films may be La-rich, which will have an influence on the properties of the 2DEG. We should point out that the La/Al ratios reported here are the nominal values obtained from 100 nm-thick LaAlO₃ films that have undergone various degrees of strain relaxation. It may or may not represent the film stoichiometry in the ultrathin LaAlO₃ layers used in the 2DEG studies. Further, the correlation between the deposition conditions and the film stoichiometry can be different for different deposition systems. Nevertheless, our result demonstrates that one needs to take into account the LaAlO₃ film stoichiometry, in addition to the oxygen vacancy effects, when studying the 2DEG properties at the LaAlO₃/SrTiO₃ interfaces using LaAlO₃ films deposited under low oxygen pressures.

IV. CONCLUSIONS

We present here the results of structural and composition characterizations of a series of 20 epitaxial LaAlO₃ films grown by PLD under different conditions. Despite the strain and strain relaxation in the LaAlO₃ films, we found that the unit-cell volume expands by as much as 4% when the film composition is La rich. The cation off-stoichiometry reaches over 50% La rich when the oxygen pressure during the deposition is 10⁻² Torr or lower. No significant effect on the composition by changing the laser energy density was observed. We conclude that the LaAlO₃ film stoichiometry is an important factor in the 2DEG properties at the LaAlO₃/SrTiO₃ interface when the LaAlO₃ film is deposited under low oxygen pressures.

Note added in proof. After the acceptance of the paper, we became aware of the paper by E. Breckenfeld *et al.*²⁶ on the effects of LaAlO₃ stoichiometry on the transport properties of the LaAlO₃/SrTiO₃ interfaces. Their result clearly demonstrate the importance of the deposition conditions of the LaAlO₃ layer on the 2-dimensional electron gas (2DEG) system properties.

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